This supplement provides some statistical details of the models for estimating individual-level utilities in the manuscript.

## **Bayesian Latent Utility Model**

Formulation and interpretation: Individual patient preferences for different attributes of Personalized Trials were estimated using empirical Bayesian latent utility modeling on all conjoint responses of the participants. Under this model, the latent utility of trial prototype j to a participant i (denoted as  $u_{ii}$ ) was postulated to follow a logistic distribution in which the mean depended on a linear combination of trial attributes. Specifically, having  $u_{ij} = \beta_i^T x_{ij} + \varepsilon_{ij}$ , where  $\varepsilon_{ij}$  is a standard logistic error and the design  $x_{ij}$  indicated the presence/absence of attributes in prototype j presented to the participant, for i=1, ..., n, and j=1, ..., J. In our application, n = 500 and J = 2. We note that  $x_{ij}$  is a vector of length equal to the number of binary attributes. For attributes with more than 2 levels (e.g. treatment types), we code  $x_{ij}$  using dummy variables. To illustrate and unpack the model formulation, consider the simplified case where we only have two binary attributes, namely, blinding (denoted as  $x_{blind,i,j}$ ) and cost (denoted as  $x_{cost,i,j}$ ) for individual i and scenario j in a question. The vector  $x_{ij} = (x_{blind,i,j}, x_{cost,i,j})^{T}$ . Then  $\beta_{blind,i}$  denotes the contribution to the utility  $u_{ij}$  due to blinding, and  $\beta_{cost,i}$  due to cost. For example, suppose the first scenario (j=1) in a conjoint question is presented with blinding  $(x_{blind,i,j} = 1)$  and no cost  $(x_{cost,i,j} = 0)$ , whereas the second question with no blinding  $(x_{blind,i,j} = 0)$  and cost  $(x_{cost,i,j} = 1)$ . Then the utility for the first scenario:  $u_{i1} = \beta_{blind,i} x_{i1} + \beta_{cost,i} x_{i1} + \varepsilon_{i1} = \beta_{blind,i} + \varepsilon_{i1}$  and the utility for the second scenario:  $u_{i2} = \beta_{blind,i} x_{i2} + \beta_{cost,i} x_{i2} + \varepsilon_{i2} = \beta_{cost,i} + \varepsilon_{i2}$ . Thus, by comparing  $u_{i1}$  and  $u_{i2}$  based on the conjoint response, we can directly compare the coefficients, with mean zero noise. In other words, the conjoint utilities provide the relative preferences between two attributes.

*Estimation method:* In a conjoint survey, while we do not observe  $u_{ij}$  directly (i.e., a latent utility), we do observe  $d_i = I(u_{i1} > u_{i2})$ , the conjoint question response. It can be easily show that  $d_i$  is binomial variable with probability that is logit-linear in  $\beta_i$ , and thus a mixed effect logistic regression *likelihood* function can be used for inference. Using the empirical Bayes formulation similar to Laird and Ware (1982), we postulate  $\beta_i$  are distributed as N(0,**D**), independently of each

other, where **D** is a positive-definite covariance matrix. Instead of prescribing what **D** is, we estimate it from the marginal likelihood of  $\{d_i\}$  after integrating out  $\beta_i$ . We note that while the formulation in Laird and Ware (1982) is described for linear mixed model, the principle naturally extends to generalized linear mixed model and the estimation method of **D** is implemented in the glmer function of the R library lme4 (Bates et al., 2015).

*General statistical analyses:* All statistical analyses in the article were performed using R Statistical Software (R Core Team, 2020).

## **Reference:**

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